On The Growth Process Of Firms: Does Size Matter?

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ABSTRACT

The purpose of this empirical study is to investigate whether the growth process of firms is best explained essentially by a random process as envisaged by Gibrat's law, or by identifiable systematic influences such as growth persistence and firm size. A dynamic random coefficients model is applied to data on 260 Canadian firms classified into four groups according to firm size. Gibrat's law of proportionate effect is not supported by the empirical results. Specifically, the findings indicate that smaller firms grow faster than larger ones in all cases. However, they also show that the effect of the disadvantage of size on growth is somewhat different for each group.

Keywords: Firm Size; Growth Persistence; Gibrat's Law; Random Coefficients Model

INTRODUCTION

s the growth process of firms best explained by identifiable systematic influences, or is it essentially a random process? Numerous studies have dealt with this empirical issue, which was first addressed by Robert Gibrat (1931). In his seminal study, Gibrat demonstrated that the skewed distributions of enterprise and plant sizes in the French manufacturing establishments can be explained very well by a random growth process. This assumption of random growth has been subsequently christened the Gibrat's law of proportionate effect. To be more specific, Gibrat's law implies that with a random growth process, the expected growth rate of a firm is independent of its size and other identifiable and industry characteristics. The issue of whether firm size has a systematic influence on the growth rate of a firm has been the subject of extensive investigation in empirical studies because this size-growth relation is most directly involved in explaining the size-distribution of firms. Following Simon (1955), several studies have used the Gibrat's law to explain the size-distribution of the large firms in the United States. See, for instance, Iriji and Simon (1974, 1977) and Vining (1976), and Sutton (1997) for discussions on the theory and empirical studies.

The empirical evidence on Gibrat's law is mixed; see for instance Nassar et al. (2013). In some empirical studies, there is support for Gibrat's law while the law does not exactly hold in some other studies. As examples, Evans (1987) reported a negative relation between size and the growth rate among a large sample of U.S. firms, while Hall (1987), also studying U.S. firms, found that Gibrat's law held for the larger firms, and that size had a weak positive effect on growth for the smaller firms. This lack of robustness in empirical results on the size-growth relationship is also evident from UK data. A study of UK firms by Singh and Whittington (1975) showed a mildly positive relationship between firm size and growth, while that of Kumar (1985) found a weak negative effect of size on growth. In another study of UK firms, Hart and Oulton (1996) found that among surviving companies during the 1989-93 period, only the very small companies grew faster; among the remaining companies there was little tendency for the proportionate growth of the firm to vary with its size. Studies involving large international firms similarly reveal conflicting results on the size-growth relationship. See for instance, Droucopoulos (1982, 1983), and Buckley, Dunning, and Pearce (1984). Nevertheless, the simulation models formulated by Nelson and Winter (1978, 1982a, 1982b) indicate that larger firms have a higher expected growth rate that is attributable to their research advantage in technological competition. The basis of suspecting such an influence is rooted in the well-known Schumpeterian hypothesis. This hypothesis suggests that bigger firms have an advantage in the R&D process in that these firms enjoy an economy of scale in the R&D effort and also have a superior ability to exploit the results of research, see Schumpeter (1950), and Kamien and Schwartz

(1982). In other words, it seems reasonable to expect that this Schumpeterian research advantage would lead to a faster growth for the bigger firms. AmirKhalkhali and Mukhopadhyay (1993) examined both the growth rates and the size-distributions of a sample of firms in the USA during the 1965-1987 period. The focus in that study was whether the size-growth relationship depends on whether or not the firms are operating in R&D- intensive industries. The study concluded that smaller firms tend to have an advantage in the growth process and that this advantage is more pronounced in the industries offering greater technological opportunities. This paper attempts to contribute to the empirical literature on the growth process of firms by applying a more general model to data on a sample of firms in Canada over the two sub-periods of 2006-2007 and 2009-2010. To be more specific, whether the growth process of these firms is best explained essentially by a random process as envisaged by Gibrat's law, or by identifiable systematic influences such as firm size and persistence of growth, is investigated empirically using a dynamic varying coefficients model.

FIRM SIZE, GROWTH, AND PROFITABILITY: A DESCRIPTIVE ANALYSIS

The sample used in this study consists of data for the same 260 firms maintaining their identity over the 2006-2010 period. These firms are chosen from the Financial Post list of 500 largest industrial firms in Canada. These firms are classified into four groups on the basis of their size measured by their sales/revenues ratios, so that each group includes 65 firms. This might create a selection bias, since the entering and exiting firms, as also the firms losing identity through merger, are eliminated. However, Hall (1987) shows that this potential bias is unlikely to be serious if the period under study is short, as is the case in this study.

Table 1 provides some information about the average firm size, measured by their sales, in all firms as well as in each group over two selected years, 2007 and 2010. It shows a slight increase in the average size of firm from 2007 to 2010 despite the 2008 worldwide financial crisis. It also points out that the average firm size of Group I is significantly larger than that of the sample as a whole, while that of the other three groups falls below the sample average in both years. Table 2 presents a summary measure of firm size inequality, as indicated by the coefficient of variation. It shows that the first group has the highest concentration. However, the firm size inequality coefficients followed a decreasing trend, i.e., less concentration in 2010 relative to 2007, especially for the three smaller firm size groups.

Table 1. Average Size of Firms (In Million Dollars)

Period	All Firms	Group I	Group II	Group III	Group IV
2007	3,813	11,348	2,221	1,023	659
2010	4,040	12,106	2,348	1,098	610

Table 2. Size Inequality Coefficients

Period	All Firms	Group I	Group II	Group III	Group IV
2007	1.65	0.78	0.69	0.47	0.33
2010	1.60	0.74	0.25	0.18	0.20

Table 3 gives average growth rates for each group as well as all firms over the two sub-periods under study. It shows that the three smaller groups enjoyed growth rates in the range of 15-16%, outperforming the largest firm size group during 2006-2007. However, all groups faced with slower growth rates over the 2009-2010 period. This could be an indicator of the slow recovery after the economic crisis of 2008 and the recession of 2009. Nevertheless, Group III performed better than the other groups and still enjoyed a double digit growth rate.

Table 3. Average Growth Rates of Firms (%)

Period	All Firms	Group I	Group II	Group III	Group IV
2006-2007	14.30	11.12	15.81	15.10	15.02
	(0.41)	(0.15)	(0.44)	(0.27)	(0.61)
2009-2010	8.91	6.37	9.66	13.99	5.59
	(0.22)	(0.18)	(0.15)	(0.33)	(0.16)

^{*}Figures in brackets are standard deviations.

Table 4 provides information about the average profitability, measured by profits/sales ratios, for each group as well as all firms over the two selected years, 2007 and 2010. It shows no significant change in the overall average profitability in 2010 compared with that of 2007. However, while profitability slightly increased in the case of Group II, it jumped significantly for Group III but decreased in the cases of Group I and Group IV.

Table 4. Average Profitability of Firms (%)

Period	All Firms	Group I	Group II	Group III	Group IV
2007	10.8	14.3	15.0	10.5	7.1
2010	10.4	13.4	15.1	17.6	5.8

Table 5 reports the period-wise bivariate correlation coefficients between firm size (Y), growth (G), and profitability (P) for all firms pooled together as well as for each of the four groups of firms. Note that subscripts t-l and t refer to the beginning-of-the-period and the end-of-the-period values of the variable, respectively. The correlations between G_t and Y_{t-1} are negative, indicating the disadvantage of size. However, these coefficients are not statistically significant in the cases of Group I and Group IV. The reported significant correlations between P_t and P_{t-1} imply persistence of profits in all cases. According to Mueller (1977, 1986), firms use their current profits to protect future profits, employing various means such as product differentiation and ownership of scarce human and natural resources. This endogenous theory of the persistence of profit is also consistent with theories and empirical studies relating persistently high profit rates to market structural variables. The correlation results between G_t and G_{t-1} also point to autocorrelated or persistent growth in all cases except for Group III. The persistence of growth may arise due to special talents or circumstantial advantages available to some growing firms who continue to enjoy a higher-than-average growth rate. See, Singh and Whittington (1975) and Chesher (1979). Note that the persistence of growth is in violation of Gibrat's law that growth of firms is random, and thus, is independent of systematic influences such as past growth rates.

Table 5. Correlation Analysis: Firm Size, Growth, And Profitability

		Y _{t-1}	G_{t-1}	G _t	P _{t-1}
	G_{t-1}	-0.0497	- 1-1	- 1	t-1
All Firms	G_{t}	-0.1285*	0.1279*		
	$\mathbf{P_{t-1}}$	0.1032	0.0487	0.0554	
	$\mathbf{P_t}$	0.0585	0.0854	-0.0042	0.6352*
	G _{t-1}	-0.0682			
C I	G_{t}	-0.1451	0.4169*		
Group I	$\mathbf{P_{t-1}}$	-0.1173	0.3266*	0.0449	
	$\mathbf{P_t}$	-0.2082	0.2786*	0.0024	0.7457*
	G_{t-1}	-0.2407*			
Casum II	G_{t}	-0.2748*	0.2477*		
Group II	P_{t-1}	-0.0742	0.0830	-0.2097	
	$\mathbf{P_t}$	0.0304	0.1289	-0.2047	0.7750*
	G_{t-1}	-0.0644			
C III	G_{t}	-0.4031*	0.0960		
Group III	P_{t-1}	-0.0565	0.2085	0.2094	
	$\mathbf{P_t}$	0.0291	0.0009	0.008	0.4933*
	G_{t-1}	0.1887			•
Casum IV	G_{t}	-0.0207	0.2497*		
Group IV	$\mathbf{P_{t-1}}$	0.0194	0.1030	-0.021	
	$\mathbf{P_t}$	-0.1419	0.0937	0.090	0.5082*

^{*}Denotes significantly different from zero at the 0.05 level or less.

THE MODEL, THE ESTIMATION STRATEGY, AND EMPIRICAL RESULTS

Consider first the following log linear regression model for testing Gibrat's law of proportionate effect for a set of firms surviving over a period of time:

$$\ln \mathbf{Y}_{ijt} = \alpha_1 + \alpha_2 \ln \mathbf{Y}_{ijt-1} + \mathbf{u}_{ijt} \tag{1}$$

where Y_{ij} represents the size of the i^{th} firm in the j^{th} group. As noted before subscripts t-l and t refer to the beginning-of-the-period and the end-of-the-period values of Y, respectively. α_1 and α_2 are parameters, and u's are the stochastic disturbances.

In this model, the Gibrat's law of proportionate effect holds if $\alpha_2 = 1$, i.e., firm growth is independent of size. If $\alpha_2 < 1$, smaller firms are expected to grow faster, and if $\alpha_2 > 1$ then the opposite would be true. However, the estimation of this model by ordinary least squares (OLS) would be open to serious question if, as is likely, there is serial correlation in the random term u_{ijt} , see for example Chesher (1979). Define the growth rate of the i^{th} firm in the j^{th} group at time t as $G_{ijt} = (Y_{ijt} - Y_{ijt-1})/Y_{ijt-1}$ and using Taylor expansion then combining with equation (1) it approximately holds that

$$G_{ijt} = \alpha_1 + (\alpha_2 - 1) \ln Y_{ijt-1} + u_{ijt}$$
 (2)

On the basis of the assumption that the u's are generated by the first- order autoregressive scheme,

$$G_{ijt} = \alpha_1(1 - \rho) + (\alpha_2 - 1)(1 - \rho) \ln Y_{ijt-1} + \alpha_2 \rho G_{ijt-1} + V_{ijt}$$
(3)

where ρ is the coefficient of autocorrelation and v's are serially uncorrelated. Now let $\beta_1 = \alpha_1$ (1- ρ), $\beta_2 = (\alpha_2 - 1)(1-\rho)$, and $\beta_3 = \alpha_2 \rho$. This yields

$$G_{iit} = \beta_1 + \beta_2 \ln Y_{iit-1} + \beta_3 G_{iit-1} + V_{iit}$$
(4)

The model expressed in equation (4) can now be used to conduct direct tests concerning the relationship between firm growth rate and its initial size as well the persistence of growth. However, if the ordinary least squares estimation method is used, any test about the parameters would be open to serious question if, as is likely, there is heteroscedasticity in the disturbance term; see for example Prais (1976), Chesher (1979), and Jovanovic (1982). In the above model, managerial/organizational differences among these firms are assumed away by virtue of the assumption that all coefficients are the same across these firms. This is a questionable assumption a priori; at least one that should be treated as a testable proposition. Following AmirKhalkhali and Dar (1993), this paper deals with these issues by adopting the more general varying coefficients model, which treats the fixed-coefficients assumption as a testable proposition. In addition, the varying coefficients model can be seen as a refinement of the stochastic law relating growth to its main determinants [see Pratt and Schlaifer (1988)]. Accordingly, the following model is estimated in this study:

$$G_{ijt} = \beta_{1j} + \beta_{2i} \ln Y_{ijt-1} + \beta_{3i} G_{ijt-1} + \varepsilon_{ijt}$$
(5)

Note that (5) is a varying coefficients model, and that the new disturbance term is not the joint effect of excluded variables; instead, it is the joint effect of the remainder of the excluded variables after the effect of included variable has been factored out. The varying coefficients model represented by (5) is more general than those employed in previous studies because not only it describes more correctly the law relating the dependent variable to its determinant, but it also permits the impact to be group-specific.

The varying coefficients model (5) is estimated by applying the random generalized least squares (RGLS) methods suggested by Swamy (1970) for the pooled sample over the two periods of 2006-2007 and 2009-2010. The pooled RGLS results are presented in Table 6.

Table 6. Pooled RGLS Results: $G_{iit} = \beta_{1i} + \beta_{2i} \ln Y_{iit-1} + \beta_{3i} G_{iit-1} + \epsilon_{iit}$

FIRMS	β_1	eta_2	β_3
Pooled	1.4564	-0.0981	0.0965
	(1.0985)	(0.0782)	(0.1403)

^{*}Figures in brackets are standard errors.

The reported results in Table 6 show that the null hypothesis of no relationship between size and growth embodied in the law, i.e., β_2 =0, as well as the persistence of growth, i.e., β_3 =0 cannot be rejected for pooled data. In other words, these pooled results support Gibrat's law. It also reports a statistically significant G-Statistic. The G-statistic, which follows χ^2 distribution, rejects the null hypothesis of fixed coefficients and supports the application of varying coefficients approach in this case. In other words, the RGLS pooled results in Table 6 do not refute Gibrat's law but point to differences among the four groups. In light of this, the Swamy and Mehta (1975) RGLS method is used to estimate the varying coefficients model for each group over the two periods of 2006-2007 and 2009-2010. For more details of the RGLS estimation method and G-statistic, see AmirKhalkhali and Dar (1993), and Swamy and Tavlas (1995, 2002).

Table 7. Group-Wise RGLS Results: $G_{iit} = \beta_{1i} + \beta_{2i} \operatorname{Ln} Y_{iit-1} + \beta_{3i} G_{iit-1} + \varepsilon_{iit}$

FIRMS	eta_{1i}	eta_{2i}	β_{3i}
Group I	0.5057*	-0.0302	0.3748*
Group II	1.1130*	-0.0713*	0.0783
Group III	2.9054*	-0.2723*	-0.1374
Group IV	0.3017	-0.0187	0.0701*

^{*}Denotes significantly different from zero at the 0.05 level or less.

Table 7 reports the RGLS group-wise results. These results appear to shed more light on the somewhat aggregate results of Table 6. For more details of the RGLS estimation method and G-statistic, see AmirKhalkhali and Dar (1993), and Swamy and Tavlas (1995, 2002).

The results presented in Table 7 show that Gibrat's law does not hold in the cases of all four groups because of the significance of the impact of size (Group II and Group III) or that of the persistence of growth (Group I and Group IV). The negative results for β_{2j} imply faster growth for smaller firms than larger ones in all cases. Nevertheless, Table 7 shows that the degree of disadvantage of size on growth appears to be somewhat different for each group. It reports the largest negative impact of size on firm growth for Group III and the smallest impact for Group IV. However, it also shows a very small and insignificant impact of size on growth as well as a very large and significance persistence of growth for Group I.

SUMMARY AND CONCLUDING REMARKS

This paper attempts to contribute to the accumulating empirical literature on the growth process of firms by testing the Gibrat's law of proportionate effect, an empirical proposition stating that the growth of firms is random. To this end, a sample consisting of 260 Canadian firms that maintained their identity over the 2006-2010 period is used. These firms are divided into four size-groups and a dynamic varying coefficients model is employed. The varying coefficients approach deals properly with the problem of econometric endogeneity and is also a more general way of incorporating unmeasured differences among these firms. These results were also supported by the size-distribution results, which refute the Gibrat's law. This is not to deny that larger firms may have certain advantages in the process of research and in the exploitation of its results. These large firms may have a greater propensity to survive but they have a tendency to grow slower, and clearly, smaller firms have advantages in some other ways. It is well known that the entry of smaller firms takes away market shares from the larger firms in the presence of technological opportunity in a growing market, see, Mukhopadhyay (1985). Acs and Audretsch (1988) and Audretsch (1995) have explored how the innovative advantage differs between large and small firms in the research-oriented industries. Their analysis follows Nelson and Winter (1982) and Gort and Klepper (1982) who contend that in some industries the underlying knowledge conditions favor the larger firms whereas the opposite is true in other industries. The former is

the case of the routinized regime, while the latter case is termed the entrepreneurial regime. However, it should be noted that the growth of firms could be explained by systematic forces if one could identify special resources and opportunities generating this growth. Valuable insights may be gained by such micro-studies.

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